

9.38

The pressure due to the water at the bottom of a pool of depth h is $P_1 = \rho gh$, where ρ is the density of water. Thus from Eq. (9.3) we get the force F_1 due to the water exerted vertically on the bottom of the pool of area A :

$$\begin{aligned} F_1 &= P_1 A = \rho gh A \\ &= (1.00 \times 10^3 \text{ kg/m}^3)(9.81 \text{ m/s}^2)(3.0 \text{ m})(5.0 \text{ m} \times 10 \text{ m}) \\ &= 1.5 \times 10^6 \text{ N.} \end{aligned}$$

9.85

Consider an iceberg of volume V , whose weight is given by $F_w = \rho_{\text{ice}} g V$. If the volume of the submerged portion of the iceberg is V_i , then according to Eq. (9.9) the buoyant force exerted on it by the sea water (of density ρ_s) is $F_b = \rho_s g V_i$. For the iceberg to be in mechanical equilibrium F_w and F_b must be equal: $F_w = \rho_{\text{ice}} g V = F_b = \rho_s g V_i$, which gives $V_i/V = \rho_{\text{ice}}/\rho_s$. The fraction of the volume of the iceberg submerged is V_i/V ; hence the fraction of its volume that is visible (i.e. above the sea level) is given by

$$1 - \frac{V_i}{V} = 1 - \frac{\rho_{\text{ice}}}{\rho_s} = 1 - \frac{0.92 \times 10^3 \text{ kg/m}^3}{1.025 \times 10^3 \text{ kg/m}^3} = 0.10 = 10\%.$$

For fresh water, replace ρ_s with $\rho_w = 1.00 \times 10^3 \text{ kg/m}^3$ in the formula above to obtain the new value of the fraction. The answer is 8.0%.

9.118

Consider a tube of flow of the air which starts far from the building, where $P = P_A$ and $v = v_A$ and ends up at the top of the roof (T), where $P = P_T$ and $v = v_T$. Apply Bernoulli's Equation: $P_A = P_T + \frac{1}{2} \rho v_T^2$, where $\rho = 1.1 \text{ kg/m}^3$ is the density of the air and $v_T = 50 \text{ m/s}$ is the air speed. Inside the building the air is not moving so the pressure at the bottom of the roof is just P_A . The net upward pressure exerted on the roof is then $\Delta P = P_A - P_T = P_A - (P_A - \frac{1}{2} \rho v_T^2) = \frac{1}{2} \rho v_T^2$ which results in an upward lifting force F_l on the roof of area A :

$$F_l = A \Delta P = \frac{1}{2} A \rho v_T^2 = \frac{1}{2} (220 \text{ m}^2)(1.1 \text{ kg/m}^3)(50 \text{ m/s})^2 = 3.0 \times 10^6 \text{ N,}$$

which is equivalent to $68 \times 10^3 \text{ lb}$.

9.119

Apply Bernoulli's Equation to points 2 and 3: $P_2 + \frac{1}{2} \rho v_2^2 + \rho g y_2 = P_3 + \frac{1}{2} \rho v_3^2 + \rho g y_3$. Note that $v_2 = \sqrt{2gh}$ [see Problem (9.111)]. Also, $y_2 = 0$, $y_3 = y$, and $P_2 = P_3 = P_A$ (since the water at both locations are exposed to the air). Substitute these expressions into Bernoulli's Equation to obtain

$$P_A + \frac{1}{2} \rho (\sqrt{2gh})^2 = P_A + \frac{1}{2} \rho v_3^2 + \rho g y.$$

Solve for v_3 : $v_3 = \sqrt{2g(h-y)}$. So obviously y cannot exceed h . This is expected from conservation of mechanical energy between points 1 and 3. To express y in terms of v_3 and θ note that $v_3 = v_2 \cos \theta = \sqrt{2g(h-y)}$, which we solve for y :

$$y = h - \frac{v_3^2 \cos^2 \theta}{2g} = \frac{v_2^2 - v_3^2 \cos^2 \theta}{2g} = \frac{v_2^2 \sin^2 \theta}{2g} = \frac{(2gh) \sin^2 \theta}{2g} = h \sin^2 \theta,$$

where we used $v_2^2 = 2gh$ and $1 - \cos^2 \theta = \sin^2 \theta$.