

2.4

From Eq. (9.1) we find the mean density of the Earth to be

$$\rho_e = \frac{M_e}{V_e} = \frac{M_e}{\frac{4\pi}{3}R_e^3} = \frac{3(5.975 \times 10^{24} \text{ kg})}{4\pi(1.274246 \times 10^7 \text{ m}/2)^3} = 5.515 \times 10^3 \text{ kg/m}^3.$$

Now change ρ_e to ρ_n , the density of nuclear matter, and solve for the corresponding new radius R'_e from the equation above:

$$R'_e = \left(\frac{3M_e}{4\pi\rho_n} \right)^{1/3} = \left[\frac{3(5.975 \times 10^{24} \text{ kg})}{4\pi(2 \times 10^{17} \text{ kg/m}^3)} \right]^{1/3} = 2 \times 10^2 \text{ m},$$

which is only about one-eighth of a mile.

2.5

The molar mass of water is 18 g/mol. Thus the number of water molecules contained in 1.00 g of water is $[1.00 \text{ g}/(18 \text{ g/mol})](6.02 \times 10^{23} \text{ /mol}) = 3.34 \times 10^{22}$. Since each H_2O molecule contains 3 atoms, the number of atoms in 1.00 g of H_2O is $3(3.34 \times 10^{22}) = 1.00 \times 10^{23}$, regardless of whether it is in liquid or solid state.

A mass of a water molecule is 18.0 u, of which 2.0 u, or $2.0 \text{ u}/18.0 \text{ u} = 1/9$, is hydrogen. Thus the weight of hydrogen in 62.4 lb of water is $(1/9)(62.4 \text{ lb}) = 6.93 \text{ lb}$, which corresponds to a mass of $(6.93 \text{ lb})(0.4536 \text{ kg/lb}) = 3.14 \text{ kg}$.

2.24

On the one hand, when the fluid level is at height h above the bottom of the tank, the fluid surface assumes a circular area of radius $r = \frac{1}{2}h$. The volume of the water in the tank at that moment is $V = \frac{1}{2}\pi r^2 h = \frac{1}{12}\pi h^3$. The time rate of change of V is then

$$\frac{dV}{dt} = \frac{d}{dt} \left(\frac{1}{12}\pi h^3 \right) = \frac{1}{4}\pi h^2 \left(\frac{dh}{dt} \right).$$

On the other hand, we know that the volume of the water changes because water is being poured into the tank at the rate of $dm/dt = \mu$, in kg per sec. Since $V = m/\rho$, we may divide μ by ρ , the density of water, to obtain the rate at which the volume of the water changes due to the addition of the water:

$$\frac{dV}{dt} = \frac{d(m/\rho)}{dt} = \frac{1}{\rho} \frac{dm}{dt} = \frac{\mu}{\rho}.$$

Equate the two expressions above for dV/dt to obtain $\frac{1}{4}\pi h^2 (dh/dt) = \mu/\rho$, or

$$\frac{dh}{dt} = \frac{4\mu}{\pi h^2 \rho}.$$

2.26

Use Eq. (9.4): $P_1 = \rho gh$. Here $P_1 = 400 \text{ kPa}$ and $\rho = 1.000 \times 10^3 \text{ kg/m}^3$, so the height of the water column is

$$h = \frac{P_1}{\rho g} = \frac{400 \times 10^3 \text{ N/m}^2}{(1.000 \times 10^3 \text{ kg/m}^3)(9.81 \text{ m/s}^2)} = 40.8 \text{ m}.$$