

11.4

The speed of the wave is given by $v = 10 \text{ m}/2.0 \text{ s} = 5.0 \text{ m/s}$. Thus from Eq. (11.1)

$$f = \frac{v}{\lambda} = \frac{5.0 \text{ m/s}}{0.50 \text{ m}} = 10 \text{ Hz.}$$

11.8

Again, compare the given waveform $y = (10 \text{ cm}) \sin(2\pi x/0.0314 \text{ cm})$ with the expression Eq. (11.2) to obtain $\lambda = 0.0314 \text{ cm} = 3.14 \times 10^{-4} \text{ m}$. Thus the period is

$$T = \frac{1}{f} = \frac{\lambda}{v} = \frac{3.14 \times 10^{-4} \text{ m}}{4.00 \text{ m/s}} = 7.85 \times 10^{-5} \text{ s} = 78.5 \mu\text{s}.$$

11.10

Start with Eq. (11.3), $\psi = A \sin[(2\pi/\lambda)(x - vt)]$. Since $k = 2\pi/\lambda$ we have

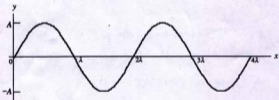
$$\psi = A \sin \frac{2\pi}{\lambda} (x - vt) = A \sin k(x - vt) = A \sin(kx - kv t),$$

where in the last expression $kv = (2\pi/\lambda)v = 2\pi/(\lambda/v) = 2\pi/T = 2\pi f = \omega$. So

$$\psi = A \sin k(x - vt) = A \sin(kx - \omega t).$$

11.22

At $t = 0$, $y = A \sin 2\pi(x/\lambda)$ and it has the corresponding values of 0, 0.707A, A, -A, -0.707A, 0. The profile is plotted below.



By comparison, at $t = 0$ $y' = A \sin 2\pi(-x/\lambda) = -A \sin 2\pi(x/\lambda) = -y$ and it has the corresponding values of 0, -0.707A, -A, 0.707A, A, 0.707A, 0. Notice that changing of the phase changes the sign of the sine function: $\sin(-\varphi) = -\sin \varphi$. The profiles are shifted 180° to one another. y' is plotted below.

